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Tuning valley-Ohmic contacts and interfacial electronic properties in valley-polarized semiconductor/Dirac semimetal heterostructures†

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Understanding and modulating the contacts and valley states in valley-polarized electronic devices is essential for designing next-generation valleytronic computing and memory devices. In this work, a class of van der Waals heterostructures (vdWHs) based on the valley-polarized semiconductor GdI2 and Dirac semimetals X (graphene, germanene, and SiGe) is designed, achieving intrinsic p-type Ohmic contacts with precise modulation of the interfacial electronic properties. Using density functional theory calculations, we reveal that X/Gdl₂ vdWHs induce a significant band gap in the Dirac semimetals due to interlayer orbital hybridization. Additionally, the graphene/Gdl₂ vdWH exhibits an intrinsic p-type halfvalley Ohmic contact, while germanene/Gdl₂ and SiGe/Gdl₂ vdWHs form intrinsic p-type overall Ohmic contacts. Due to work function differences, the contact interfaces between Gdl₂ and X result in a builtin electric field, as evidenced by the calculated charge density differences and electrostatic potentials. Furthermore, by adjusting the interlayer distance and applying electrostatic doping, the Schottky barrier heights and valley splitting in X/GdI₂ vdWHs can be precisely tuned, which facilitates transitions from a half-valley Ohmic contact to an overall Ohmic or Schottky contact, achieving valley-switching ON/OFF states at K and K' points. This study provides strategies for realizing multi-state valley-polarized electronic devices through interface engineering of valley-polarized semiconductors and Dirac semimetals.

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1. Introduction

Quantum materials with engineered magnetic orders and topological states have opened exciting opportunities for next-generation spintronic devices. ¹⁻⁴ In particular, two-dimensional (2D) valley-polarized materials stand out due to their distinctive physical and electronic characteristics, offering significant potential for spintronic and valleytronic applications. ⁵⁻⁷ Unlike conventional 2D semiconductors, where the electronic properties are governed mainly by carrier density, valley-polarized semiconductors provide additional control through valley polarization states (K and K'), providing extra electronic degrees of freedom. ^{8,9} The coupling between valleys and spin degrees of freedom in 2D materials has led to significant advancements in valleytronics and spintronics,

especially for devices that utilize spontaneous valley polarization. This spin-valley coupling results in spin-valley locking, enabling selective control of spin and valley states for encoding and reading information. 10 Such a relationship provides unique opportunities for designing spintronic and valleytronic devices, offering advantages in multi-state storage and low-power information processing.⁵ In recent years, numerous 2D materials with valley polarization have been reported, such as MX (M = Zr, Ru, Os; X = F, Cl, Br, I), $^{11-14}$ MI_2 (M = Sc, Y), ¹⁵ CeX_2 (X = F, Cl, Br), ¹⁶ GdX_2 (X = Cl, Br, I), ¹⁷⁻¹⁹ and transition-metal dichalcogenides (TMDs) under circularly polarized light.20 Among them, the GdI2 monolayer stands out for its remarkable valley splitting (149 meV) and high Curie temperature (241 K),²¹ resulting from the joint effects of d-orbital magnetic exchange interactions and the f-orbital strong spin orbital coupling effect of the Gd atom. With its pronounced valley polarization and elevated Curie temperature, the GdI2 monolayer holds great potential for forming an intrinsic half-valley Ohmic contact with semimetals at room temperature. Notably, the layered vdW bulk GdI₂ has already been successfully synthesized experimentally.²² Due to its lower cleavage energy (0.26 J m⁻²)²¹ than that of graphene (0.36 J m⁻²),²³ the GdI₂ monolayer is highly likely to be exfoliated and easily transferred, demonstrating strong experimental feasibility for constructing valley-polarized logic devices.

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Additionally, the electronic states of different valleys in 2D valley-polarized semiconductors exhibit distinct symmetry differences in the band structure, which can be tuned by external factors such as electric field, 24,25 magnetic field, 33,26 and strain engineering. 18,27-29 In valleytronics, accurately controlling valley polarization modulates electronic transport, enabling precise adjustment of device switching characteristics and performance, which is crucial for the development of nextgeneration valleytronic computing and memory technologies. For instance, monolayer SnS, due to its intrinsic electric field and tunable Berry curvature, can exhibit significantly enhanced valley-spin splitting and Berry curvature under biaxial compressive strain, thereby enhancing the stability of valley polarization and expanding the valleytronic material system with elastic tunability. 30 Another study revealed that constructing ScI₂/MSe₂ (M = Zr, Hf, Sn) heterostructures can induce a transition from in-plane to out-of-plane magnetization, significantly enhancing valley splitting up to 121 meV and greatly improving valley polarization performance.³¹ Moreover, in a WSe₂/Fe₃GeTe₂ van der Waals heterostructure (vdWH), efficient injection of spinpolarized holes under bias induces significant valley polarization between the $\pm K$ valleys, demonstrating promising potential for application in scalable, room-temperature valleytronic devices and magneto-optoelectronic integration.³²

However, integrating 2D materials into practical devices, particularly in the design and optimization of contact interfaces, remains challenging.33-37 For example, in vdWHs formed between 2D semiconductors and monolayer metals, highthroughput calculations reveal that the Schottky barrier height (SBH) and contact type are primarily governed by the interfacial potential difference, charge transfer, and interfacial dipole moments.³⁸ Very recently, Ang et al. proposed the concept of half-valley Ohmic contact in the RuCl₂/graphene vdWH by hole doping, enabling precise carrier control by allowing current injection through the 'Ohmic valley' at low-dissipation, while suppressing it at the 'Schottky valley'. 39 This approach introduces a new tunable degree of freedom for regulation: valleyswitching states, which are crucial for advancing valleytronic devices. Therefore, understanding and modulating the physical properties of the contact interfaces between valley-polarized semiconductors and metal electrodes are crucial for the practical applications of 2D valley-polarized semiconductors in multi-state computing, storage, and spintronics.

Here, we present a class of X/GdI₂ vdWHs, consisting of 2D Dirac semimetals X (X = graphene, germanene, and SiGe) and a GdI₂ monolayer with significant valley splitting. By exploring different atomic alignments, we constructed three distinct stacking modes for each X/GdI2 vdWH, with the T1-type stacking mode showing the lowest binding energy and being identified as the most stable configuration. Upon interaction with GdI₂, the Dirac points of the Dirac semimetal X open large band gaps. When spin-orbit coupling (SOC) is considered, the projected band structures show that the graphene/GdI2 vdWH exhibits intrinsic p-type half-valley Ohmic contacts, while both germanene/GdI2 and SiGe/GdI2 vdWHs form intrinsic p-type overall Ohmic contacts. The charge redistribution and built-in

electric field at the interface induced by the work function difference between GdI2 and Dirac semimetals are confirmed by the charge density difference and electrostatic potential. Furthermore, by modifying the interlayer distance and implementing electrostatic doping, the SBHs of X/GdI2 vdWHs can be precisely tuned, enabling transitions between half-valley Ohmic contacts, overall Ohmic contacts, and overall Schottky contacts. Finally, we discuss the regulation of charge injection and valleyswitching ON/OFF behavior in potential spintronic devices based on X/GdI2 vdWHs under external fields. This study provides a novel perspective on valley-polarized semiconductors and offers theoretical guidance for designing low-power spintronic devices.

2. Methods and computational details

First-principles calculations were performed using density functional theory (DFT) as implemented in the Vienna ab initio Simulation Package (VASP). 40,41 The projector augmented wave (PAW) pseudopotentials⁴² with valence electron configurations of $4f^75d^16s^2$ for Gd, $5s^25p^5$ for I, $2s^22p^2$ for C, $3s^23p^2$ for Si, and 4s²4p² for Ge were employed to describe ion-electron interactions. The exchange-correlation functional was described using the generalized gradient approximation (GGA) with the Perdew, Burke and Ernzerhof (PBE) functional. 43 The HSE06 hybrid functional was used to calculate the band structure of monolayer GdI2 in order to check the reliability of the electronic structure obtained from the PBE+U method. A vacuum space of 30 Å was added along the z-direction to eliminate the interaction between adjacent layers. The cutoff energy for the plane wave basis was set to 500 eV. The first Brillouin zone was sampled using a converged Γ -centered k-point mesh of size $15 \times 15 \times 1$ for structural relaxation and electronic analyses. The geometrical structures were fully relaxed until the forces and energies converged to 0.01 eV \mathring{A}^{-1} and 1.0 \times 10⁻⁵ eV, respectively. Due to the strong correlation effects of Gd-4f electrons in the GdI₂ layer, the GGA+U method⁴⁴ was used to describe its magnetic anisotropy of the GdI2 layer. The Hubbard U parameter was set to 4.6 eV. 18 van der Waals density functional correction within the Grimme scheme (DFT-D3) was implemented to account for the van der Waals interaction. 45,46 SOC was considered for the calculation of projected band structures.

Results and discussion

3.1. Structural parameters and stabilities

The GdI₂ monolayer has a 2H-MoS₂ type hexagonal crystal structure with a p6m2 space group and an I-Gd-I sandwich stacking along the z-direction. ^{17,47} The relaxed lattice constants of the pristine GdI_2 monolayer are a = b = 4.14 Å, as shown in Fig. 1a, which are in good agreement with previous theoretical results (4.139 Å).¹⁷ The optimized lattice constants of graphene, germanene, and SiGe monolayers are 2.46 Å, 4.04 Å, and 3.94 Å, respectively, as listed in Table 1, which are consistent with previously reported experimental and theoretical values. 48-51 With fixed lattice constants of the GdI2 monolayer, we

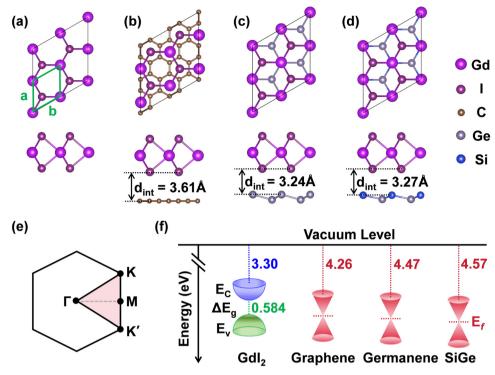


Fig. 1 Structures, Brillouin zone and band alignments. The top and side views of (a) a pristine Gdl_2 monolayer, (b) T1-type graphene/ Gdl_2 , (c) T1-type germanene/ Gdl_2 , and (d) T1-type $SiGe/Gdl_2$ vdWHs. The green rhombus denotes the unit cell of the Gdl_2 monolayer. (e) The first Brillouin zone with high-symmetry points. (f) The band alignments of Gdl_2 and Dirac semimetals X, graphene, germanene and SiGe. ΔE_g , E_C , and E_V denote the band gap, the conduction band edge, and the valence band edge of the Gdl_2 monolayer, respectively. E_f represents the Fermi level of Dirac semimetals X.

constructed the X/GdI₂ vdWHs (X = graphene, germanene, and SiGe) by stacking the 2×2 supercells of GdI₂ on the $2\sqrt{3} \times 2\sqrt{3}$ supercells of graphene, 2×2 supercells of germanene, and 2×2 supercells of SiGe with lattice mismatches of 2.90%, 2.47%, and 5.07%, respectively. The strain induced by lattice mismatch has no significant impact on the Dirac points or the overall electronic properties of the Dirac semimetals, as shown in Fig. S1 (ESI†). Moreover, owing to the different atomic alignments, we considered three different stacking modes for X/GdI₂ by shifting GdI₂ along the a and a + b directions, labeled as T1, T2, and T3, as shown in Fig. S2a-i (ESI†), respectively.

Moreover, in order to evaluate the structural stability, the binding energies (E_b) of X/GdI₂ vdWHs with different stacking modes are calculated according to the following formula:

$$E_{\rm b} = \frac{E_{\rm X/GdI_2} - E_{\rm X} - E_{\rm GdI_2}}{N} \tag{1}$$

where N = 4 is the number of GdI_2 unit cells in X/GdI₂ vdWHs; E_{X/GdI_2} , E_X , and E_{GdI_2} are the total energies of X/GdI₂ vdWHs, isolated Dirac semimetals X (X = graphene, germanene, and SiGe) and isolated GdI2 monolayer, respectively. Based on the calculated results presented in Table S1 (ESI†), all binding energies of X/GdI2 vdWHs in different stacking modes are negative, indicating that their formation is thermodynamically exothermic and easy to be synthesized experimentally. Specifically, the binding energies of T1-type graphene/GdI2, germanene/GdI₂, and SiGe/GdI₂ vdWH are -0.954 eV per atom, -0.937 eV per atom, and -0.932 eV per atom, respectively, which are lower than those of T2- and T3-type stacking modes. These results demonstrate that the T1-type stacking configurations of X/GdI2 vdWHs are more energy favorable. Therefore, we focus on and discuss the structure, electronic, and magnetic properties of T1-type X/GdI₂ vdWHs in the following sections.

Table 1 Lattice constants (a and b) of Dirac semimetals, lattice mismatches (δ) between GdI₂ and Dirac semimetals, equilibrium interlayer distances (d_{int}) and binding energies (E_{b}) of vdWHs, work functions of the Dirac semimetals (W_{m}), work functions of the vdWHs (W_{ns}) and their differences ($\Delta W = W_{\text{m}} - W_{\text{ns}}$), p-type SBHs without SOC at the K and K' points ($\Phi_{\text{p-K}/\text{K}'}$), p-type SBHs at the K point ($\Phi_{\text{p-K}}$) and the K' point ($\Phi_{\text{p-K}'}$) of the vdWHs with a positive magnetic moment along the +z-direction in the presence of SOC

vdWHs	$a = b (\mathring{A})$	δ (%)	$E_{\rm b}$ (eV)	$d_{\mathrm{int}}\left(\mathring{\mathtt{A}}\right)$	$W_{\rm m}$ (eV)	W_{hs} (eV)	ΔW (eV)	$\Phi_{\text{p-K/K}'}$ (meV)	$\Phi_{ ext{p-K}} ext{ (meV)}$	$\Phi_{\text{p-K}'}$ (meV)
Graphene/GdI ₂	2.46 2.46^{48}	2.90	-0.954	3.61	$4.26 \\ 4.24^{52}$	3.82	0.44	6	-19	130
Germanene/GdI ₂	4.04 4.034 ⁴⁹	2.47	-0.937	3.24	4.47 4.45 ⁵³	4.35	0.12	-115	-179	-37
SiGe/GdI ₂	3.94 3.939 ⁴⁹	5.07	-0.932	3.27	$4.57 \\ 4.46^{54}$	4.38	0.19	-131	-213	-64

The top and side views of optimized T1-type X/GdI₂ vdWHs are shown in Fig. 1b-d. The equilibrium interlayer distances (d_{int}) of relaxed T1-type graphene/GdI2, germanene/GdI2, and SiGe/ GdI₂ are 3.61 Å, 3.24 Å, and 3.27 Å, respectively, which are much larger than the sum of the covalent radii of I and C (Ge, Si) atoms, indicating weak vdW interactions between the GdI₂ and Dirac semimetals X.

3.2. Magnetic and electronic properties

Due to the contribution of the half-filled f and d orbitals of the Gd atom, the calculated magnetic moment of the GdI₂ monolayer is $7.434\mu_B/Gd$, which is in good agreement with the previously reported value $(7.446\mu_B/Gd)$. Fig. 1e shows the first Brillouin zone with high-symmetry points of the GdI₂ monolayer. As shown in Fig. S3a and b (ESI†), the GdI2 monolayer is a semiconductor with indirect band gap values of 1.10 eV (HSE06 + SOC) and 0.584 eV (PBE+U), which are in good agreement with the previous studies. 18,21,27 Note that the HSE06 and PBE+Ufunctionals produce quite similar band structures, with negligible differences in the band profile except for the size of the band gap. Therefore, to balance accuracy and computational efficiency, PBE+U is adopted for all calculations of monolayer GdI₂ and its vdWHs unless otherwise specified. In addition, the band structure reveals that the valley splitting of the GdI₂ monolayer is 147 meV, which is consistent with the previously reported value (149 meV)18 and larger than those of GdF2 (55 meV), GdCl₂ (38 meV), and GdBr₂ (82 meV). 19 By applying a reversed external magnetic field, the magnetization direction of the Gd atoms in the GdI2 monolayer can be effectively switched, achieving a reversal from +z to -z. As shown in Fig. S3c and d (ESI†), this magnetization reversal (M-reversing) further leads to the inversion of both spin and valley polarization

in the GdI2 monolayer, which is consistent with previous reports. 18,55

The work function, defined as the energy difference between the vacuum level and the Fermi level ($W = E_{\text{vac}} - E_{\text{f}}$), represents the minimum energy required to remove an electron from the material surface to a point in the vacuum immediately outside the material. 56,57 The work function of the isolated GdI2 monolayer is 3.67 eV, which is less than those of graphene (4.26 eV), germanene (4.47 eV), and SiGe (4.57 eV), as listed in Fig. 1f and Table 1. Due to the difference in work functions, the alignment process causes charge redistribution at the interface, thereby adjusting the work function of the vdWHs. Charge transfer at the metal-semiconductor contact interface plays a crucial role in determining the performance of electronic devices.⁵⁸ The calculations show that electrons are transferred from GdI2 to Dirac semimetals X upon the formation of their vdWHs, as illustrated in Fig. 2a-c. This behavior is opposite to what is observed in RuCl₂/graphene and NbSe₂/graphene vdWHs since the work functions of RuCl₂ and NbSe₂ are higher than that of graphene.³⁹ Consequently, the Dirac semimetals X accumulate electrons, while GdI2 experiences hole accumulation due to electron dissipation, creating a built-in electric field (E) from GdI2 to the Dirac semimetals X, as shown in Fig. 2d.

Upon stacking into vdWHs, electron transfer and redistribution at the contact interface induce alignment of the Fermi levels of GdI₂ and the Dirac semimetals, promoting the establishment of thermal equilibrium throughout the system. Specifically, the work function of the vdWHs tends to align more closely with that of the material that undergoes less carrier transfer, i.e., the material more strongly influenced by the Fermi level pinning (FLP). Here, FLP refers to an interfacial effect that arises when a metal is brought into contact with a

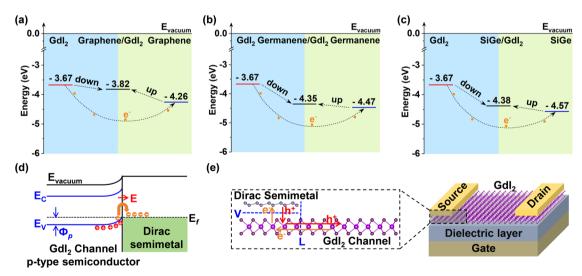


Fig. 2 Changes in the work functions and the direction of electron transfer after the formation of the X/GdI₂ vdWHs. The movement of the Fermi levels, the changes in the work functions, and the transfer direction of electrons in the process of forming (a) graphene/Gdl2, (b) germanene/Gdl2, and (c) SiGe/ Gdl_2 vdWHs. The orange dots represent the flowing electrons. (d) Schematic band diagram of the Gdl_2 channel and Dirac semimetals X. E_C and E_V denote the conduction band edge and the valence band edge of Gdl_2 in the X/Gdl₂ vdWHs, respectively. Φ_p , E_f , and E represent the p-type SBHs, the Fermi level, and the built-in electric field at the interface in X/GdI2 vdWHs, respectively. (e) Schematic of a Dirac semimetal-GdI2 contacted FET and the carrier transfer path. The blue dashed lines labeled V and L represent the vertical interface between the Dirac semimetal and the underlying GdI2 and the lateral interface between the channel GdI2 and contacted GdI2, respectively

semiconductor. A large number of surface and interface states typically exist at the metal-semiconductor interface, which can pin the Fermi level of the heterostructure at a fixed position and prevent it from being effectively tuned.³⁴ The presence of FLP weakens the ability of the metal's work function to modulate the contact barrier, leading to increased contact resistance and a reduction in overall device performance.⁵⁹ In comparison, due to its higher carrier concentration and lower density of states, graphene is more susceptible to interfacial charge transfer and Fermi level adjustment. As a result, the work function of graphene/GdI₂ (3.82 eV) is closer to that of GdI₂ (3.67 eV). In contrast, due to the lower carrier concentrations, germanene and SiGe experience greater charge redistribution at the interface, forming a stronger interfacial dipole. Consequently, FLP is more pronounced on the Dirac semimetal side, leading to the overall work functions of germanene/GdI₂ (4.35 eV) and SiGe/GdI2 (4.38 eV) being closer to those of germanene (4.47 eV) and SiGe (4.57 eV). Thus, the work function of graphene/GdI₂ is predominantly determined by GdI₂, while the work functions of germanene/GdI2 and SiGe/GdI2 are mainly governed by germanene and SiGe, respectively.

Moreover, Fig. 2d shows that electrons from the valence band of the GdI_2 monolayer transfer to the Dirac semimetals across the Schottky barrier, resulting in an increased hole concentration at the GdI_2 contact interface and the formation of holes' anti-barrier. At the same time, the energy band edges of the p-type semiconductor GdI_2 shift upward. If X/GdI_2

vdWHs form Ohmic contacts, electrons transferring from GdI_2 to the Dirac semimetals X becomes easier, free from the obstruction of the Schottky barrier. This phenomenon can be utilized to design FETs with low power consumption and high switching efficiency, as illustrated in Fig. 2e. It is worth noting that stronger interlayer interactions modify the band structure of GdI_2 , causing the energy at the Γ point in the top valence band of the spin-up channel of GdI_2 is higher than that at the K and K' points.

The SBH is a critical parameter for evaluating the interfacial charge transfer resistance of metal/semiconductor contacts. According to the Schottky–Mott rules, the n-type SBH (Φ_n) and p-type SBH (Φ_p) can be calculated using the equations:

$$\Phi_{\rm n} = E_{\rm C} - E_{\rm f}, \quad \Phi_{\rm p} = E_{\rm f} - E_{\rm V} \tag{2}$$

where $E_{\rm C}$ and $E_{\rm V}$ represent the CBM and VBM of GdI $_{\rm 2}$ in the projected band structures of the X/GdI $_{\rm 2}$ vdWHs, respectively. When 0 eV $<\Phi_{\rm n}<\Phi_{\rm p}$ or 0 eV $<\Phi_{\rm p}<\Phi_{\rm n}$, n-type or p-type Schottky contacts are formed, respectively. However, when $\Phi_{\rm n}\leq$ 0 eV or $\Phi_{\rm p}\leq$ 0 eV, n-type or p-type Ohmic contacts are established. ⁵⁸

When SOC is not considered, the schematic drawing of the band structure contributed by GdI_2 at the K and K' points in X/ GdI_2 vdWHs with no valley splitting is shown in Fig. 3a. The projected band structures of X/ GdI_2 , as shown in Fig. S4a–c (ESI \dagger), reveal that the Dirac points of Dirac semimetals X in graphene/ GdI_2 , germanene/ GdI_2 and SiGe/ GdI_2 deviate downward from the Fermi level by about 188 meV, 179 meV

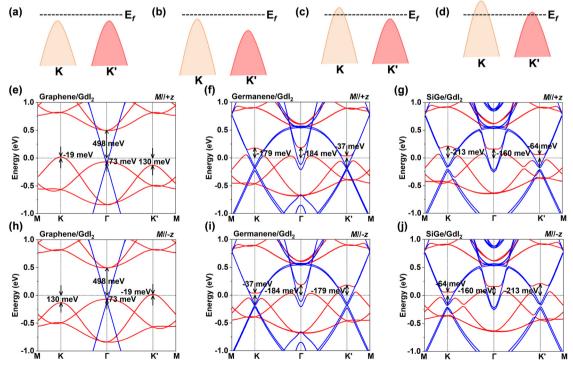


Fig. 3 Projected band structures of X/Gdl₂ vdWHs. Schematic diagrams of the band structure at the K and K' points with (a) no valley splitting, (b) p-type overall Schottky contact, (c) p-type half-valley Ohmic contact, and (d) p-type overall Ohmic contact. The brown and pink lines represent the valence band edges of Gdl₂ at the K and K' points, respectively. Projected band structures with the positive and negative magnetic moments along the z-direction of (e) and (h) graphene/Gdl₂, (f) and (i) germanene/Gdl₂, and (g) and (j) SiGe/Gdl₂ in the presence of SOC, respectively. The red and blue lines in the band structures represent the contributions from Gdl₂ and graphene, respectively. The Fermi level (E_f) is set to 0 eV.

and 185 meV, respectively. More interestingly, the exchange interaction between the electrons of the Dirac semimetals and the local magnetic moment induced by GdI2, originating from the d and f orbitals of the Gd atom, leads to a modification of the electronic structure near the Dirac point, resulting in the opening of a band gap. This interaction causes spin-up and spin-down electrons to experience distinct effective potentials, thereby giving rise to an asymmetric band gap and manifesting a spin-dependent band gap. Specifically, the spin-up (spindown) channel of GdI2 induces band gaps of 7 meV (4 meV) in graphene, 30 meV (4 meV) in germanene, and 19 meV (10 meV) in SiGe, respectively. However, since the SOC effect can induce valley splitting in the GdI2 monolayer, the X/GdI2 vdWHs may exhibit a p-type overall Schottky contact, half-valley Ohmic contact, and overall Ohmic contact at the K and K' points, as shown in Fig. 3b-d, respectively. Fig. 3e shows the p-type SBH at the K (K') point of the graphene/GdI2 vdWH is -19 meV (130 meV), while the n-type SBH at the Γ point is 498 meV. The result indicates that the graphene/GdI2 vdWH forms a p-type half-valley Ohmic contact at the K point. However, the p-type SBHs at the K and K' points of the germanene/ GdI_2 vdWH are -179 meV and -37 meV, as shown in Fig. 3f, indicating that germanene/GdI2 forms a p-type overall Ohmic contact. Similarly, the SiGe/GdI2 vdWH also exhibits a p-type overall Ohmic contact, with SBHs of -213 meV and -64 meV at the K and K' points, respectively, as shown in Fig. 3g. The p-type SBHs at the K and K' points of germanene/GdI2 and SiGe/GdI2

vdWHs are less than 0 eV, this implies that the valley polarization of GdI₂ at the K and K' points is turned off, rendering both points conductive.

The intrinsic p-type half-valley Ohmic contact (graphene/ GdI₂) and p-type overall Ohmic contact (germanene/GdI₂ and SiGe/GdI₂) are expected to have broader application in valleytronics devices than the artificially regulated half-valley and overall Ohmic contacts. More intriguingly, in the presence of SOC, the energy bands of germanene and SiGe in the X/GdI₂ vdWHs exhibit significant band splitting (blue lines), whereas graphene does not. This difference arises from the stronger interfacial hybridization between the sp² orbitals of germanene or SiGe and the orbitals of GdI2, which disrupts the equivalence of the two sublattices within the monolayers. The resulting symmetry breaking lifts the band degeneracy and causes band splitting. In contrast, the relatively weaker interfacial interaction in graphene preserves its sublattice equivalence, preventing band splitting. Moreover, by reversing the magnetization direction from +z to -z, as shown in Fig. 3h-j, the valley polarization between the K and K' points of the X/GdI₂ vdWHs can be flipped, while the absolute values of the valley splitting remain unaffected by the direction of magnetization. The reversal of out-of-plane ferroelectric polarization in the SiGe monolayer does not significantly affect the overall electronic properties or contact barrier of the SiGe/GdI2 heterostructure, which remains a p-type Ohmic contact, as shown in Fig. S5 (ESI†).

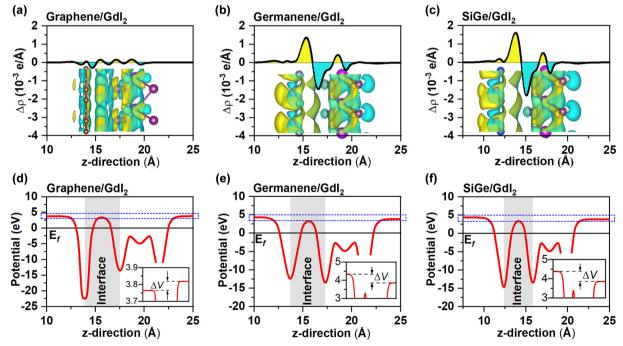


Fig. 4 Charge density difference and electrostatic potential. Plane-averaged charge density differences ($\Delta \rho$) along the z-direction of (a) graphene/Gdl₂, (b) germanene/Gdl₂, and (c) SiGe/Gdl₂ vdWHs. The insets display the 3D charge density differences. The yellow and cyan regions represent charge accumulation and depletion, respectively. The isosurface values are set to 1×10^{-5} e Å $^{-3}$. Planar average electrostatic potential curves of (d) graphene/ Gdl₂, (e) germanene/Gdl₂, and (f) SiGe/Gdl₂ vdWHs along their z-directions. The gray shaded areas represent the contact interfaces of semimetal/Gdl₂ vdWHs. The illustrations at the bottom right show partial enlargements (blue dashed lines). The Fermi level (E_f) is set to 0 eV. ΔV represents electrostatic potential difference

As previously mentioned, the construction of X/GdI_2 vdWHs disrupts the original charge balances on the surface of the Dirac semimetals and GdI_2 , causing the charge to redistribute until a new equilibrium is reached.⁶⁰ The charge redistribution at the interface between X and GdI_2 can be identified by analyzing the charge density differences $(\Delta \rho)$, defined as:

$$\Delta \rho = \rho_{\text{X/GdI}_2} - \rho_{\text{X}} - \rho_{\text{GdI}_2} \tag{3}$$

where $\rho_{X/GdI}$, ρ_X , and ρ_{GdI} , represent the charge densities of the X/GdI₂ vdWHs, the isolated Dirac semimetals X, and the isolated GdI₂ monolayer, respectively. The plane-averaged charge density differences and charge density differences of graphene/ GdI2, germanene/GdI2, and SiGe/GdI2 vdWHs are shown in Fig. 4a-c, respectively. It is evident that charge accumulation occurs on the Dirac semimetal side and depletion on the GdI₂ side, which is consistent with the direction of electron transfer previously analyzed based on the work function (Fig. 2a-c). Due to the larger interlayer distance (3.61 Å) between GdI₂ and graphene, charge transfer and dipole strength are weakened, resulting in weaker interlayer hybridization. In contrast, the smaller interlayer distances in germanene/GdI₂ (3.24 Å) and SiGe/GdI₂ (3.27 Å) lead to stronger interface hybridization, promoting charge redistribution. The different electron gain and loss of the Dirac semimetals X and the GdI2 monolayer result in the formation of dipoles at their contact interfaces, inducing an electrostatic potential difference (ΔV), as shown in Fig. 4d-f. The electrostatic potential differences (ΔV) are 0.055 eV, 0.487 eV, and 0.523 eV in graphene/GdI2, germanene/GdI2, and SiGe/GdI2 vdWHs, respectively. The combined analysis of charge density differences and electrostatic potential differences demonstrates that the charge accumulation and depletion at the germanene/GdI₂ and SiGe/GdI₂ interfaces are more pronounced than those at the graphene/GdI₂ interface, indicating a stronger interfacial dipole and enhanced charge transfer efficiency.

3.3. Tunable SBHs and valley states

Manipulating the SBHs for metal/semiconductor vdWHs is a key challenge in designing high-performance spintronic devices. Series Recent studies have shown that adjusting the interlayer distance of vdWHs is an effective method to modulate the SBH and contact type in metal/semiconductor vdWHs, including graphene/SbX (X = P, As, Bi), 61 graphene/Au₂S, 62 Ti₃X₂/MoS₂ (X = B, C, N), 63 and graphene/MTe (M = Al, B). 64 This is primarily due to the fact that the interlayer distance in 2D vdWHs determines the strength and nature of the interlayer interactions, which directly affect the SBHs. By precisely tuning the interlayer spacing, it is possible to modulate the electronic properties of the contact, including the transition between Schottky and Ohmic contacts, thereby influencing the efficiency of charge and spin transport, which is critical for the performance of high-performance spintronic devices.

As shown in Fig. 5a, the interlayer distance can be modulated by applying vertical tensile or compressive strains along the z-direction, which can be experimentally achieved through vertical pressure or by inserting a hexagonal boron nitride (h-BN) buffer layer. 61,65 Fig. 5b–d show the p-type SBHs at the K and K' points of X/GdI₂ vdWHs as a function of interlayer distances. Obviously, the p-type SBHs vary monotonically with interlayer distances, achieving a transition between negative and positive values. However, the p-type SBHs at the K point are consistently lower than those at the K' point, and the difference between them exhibits only slight fluctuations with changes in the interlayer distance, indicating that the variation

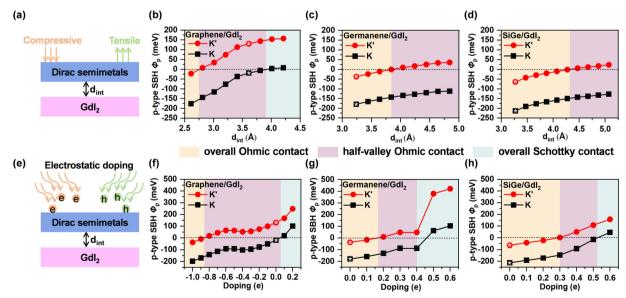


Fig. 5 Tunable p-type SBHs and contact type. (a) Schematic diagram of interlayer distance modulation through vertical compressive or tensile strains. The p-type SBHs at the K and K' points as a function of interlayer distance for (b) graphene/Gdl₂, (c) germanene/Gdl₂, and (d) SiGe/Gdl₂ vdWHs. (e) Schematic diagram of electron or hole doping. The p-type SBHs at the K and K' points as a function of electron or hole doping for (f) graphene/Gdl₂, (g) germanene/Gdl₂, and (h) SiGe/Gdl₂ vdWHs. The asterisks indicate the p-type SBHs of X/Gdl₂ vdWHs at their initial equilibrium state. The positive and negative values of electrostatic doping represent electron doping and hole doping, respectively. The magnetic moment is aligned along the +z-direction, and the SOC effect is considered.

in interlayer distances has a minimal effect on the valley polarization of GdI₂. Specifically, as shown in Fig. 5b, when the interlayer distance of graphene/GdI2 vdWH increases from 3.61 Å to more than 4.01 Å ($d_{\rm int} \geq 4.01$ Å), the p-type SBHs at both the K and K' points exceed 0 eV, indicating that the graphene/GdI2 vdWH transforms from a p-type half-valley Ohmic contact to a p-type overall Schottky contact. However, for 2.61 Å $\leq d_{\rm int} \leq$ 3.81 Å, the p-type SBH values at the K and K' points remain positive and negative, respectively, implying that the graphene/GdI2 vdWH retains an intrinsic p-type half-valley Ohmic contact. When $d_{\text{int}} \leq 2.61$ Å, the p-type SBHs at both the K and K' points of the graphene/GdI2 vdWH drop below 0 eV, forming a p-type overall Ohmic contact. The projected band structure of the graphene/GdI2 vdWH at different interlayer distances is shown in Fig. S6 (ESI†). Similarly, as shown in Fig. 5c and d, the germanene/GdI2 (SiGe/GdI2) vdWH can be transformed from the intrinsic p-type overall Ohmic contact to a p-type half-valley Ohmic contact by increasing the interlayer

distance from 3.24 Å (3.27 Å) to 3.84 Å (4.47 Å). The projected band structures of the germanene/GdI2 and SiGe/GdI2 vdWHs at different interlayer distances are shown in Fig. S7 and S8 (ESI†), respectively. When the interlayer distance is increased to about 5 Å, germanene/GdI2 and SiGe/GdI2 vdWHs remain in the p-type half-valley Ohmic contact.

External electron or hole doping is also an effective method for modulating the electronic properties of 2D materials and their vdWHs by shifting the Fermi level. 66-68 As shown in Fig. 5e, the electrostatic doping can be achieved through the application of an external gate voltage. 69,70 From Fig. 5f, one can see that the electron doping exceeding 0.1 e transforms graphene/GdI₂ vdWH from the intrinsic p-type half-valley Ohmic contact to a p-type overall Schottky contact due to the reduced p-type SBH at the K point (-19 meV). When hole doping increases from 0 e to 0.8 e, although the p-type SBHs at the K and K' points decrease with fluctuation, graphene/GdI₂ maintains the intrinsic p-type half-valley Ohmic contact.

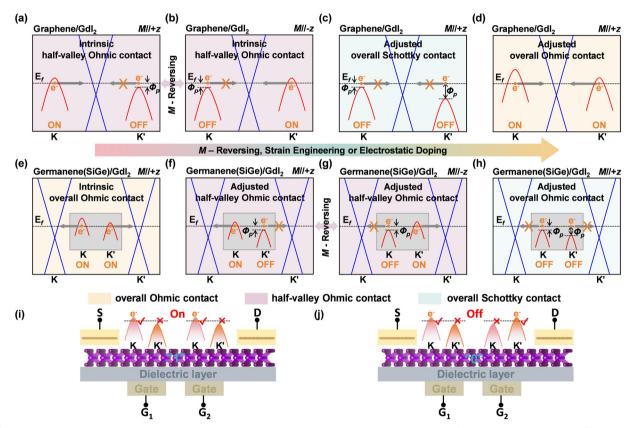


Fig. 6 Tunable contact types and valley-switching states of electronic transport. Intrinsic p-type half-valley Ohmic contact of graphene/GdI₂ vdWH with (a) +z and (b) -z magnetization directions. (c) Adjusted p-type overall Schottky contact and (d) p-type overall Ohmic contact of graphene/Gdl2 vdWH. (e) Intrinsic p-type overall Ohmic contact of germanene/Gdl2 and SiGe/Gdl2 vdWHs. Adjusted p-type half-valley Ohmic contact of germanene/Gdl2 and $SiGe/Gdl_2$ vdWHs with (f) +z and (g) -z magnetization directions. (h) Adjusted p-type overall Schottky contact of germanene/ Gdl_2 and $SiGe/Gdl_2$ vdWHs. The blue and red lines represent the energy bands with Dirac points of the Dirac semimetals X and the valence band edge of Gdl₂ in X/Gdl₂ vdWHs, respectively. The gray arrows indicate the electron transfer free paths of Gdl2 at the high-symmetry points K and K' in the X/Gdl2 vdWHs (without Schottky barrier). The orange crosses indicate that the electron transfer is blocked (with Schottky barrier). E_f and Φ_D represent the Fermi level of the X/ Gdl₂ vdWHs and the p-type SBHs at the K or K' point, respectively. The orange dots represent the freely flowing electrons. M-Reversing represents reversing the magnetization direction of Gd atoms from +z to -z. Schematic of the valley-state logic device featuring two gates, illustrating (i) the "On" state and (j) the "Off" state. S, D, and G denote the source, drain, and gate, respectively. The source and drain are in direct contact with the GdI₂ channel, while the two gates are separated from the GdI₂ channel by a dielectric layer. Dashed lines indicate the Fermi energy. The band alignment is determined by the directions of the gate electric fields

However, graphene/GdI $_2$ vdWH can be transformed into a p-type overall Ohmic contact when the hole doping reaches 0.9 e. Since germanene/GdI $_2$ and SiGe/GdI $_2$ vdWHs exhibit intrinsic p-type overall Ohmic contacts, regulation of their SBHs and contact types can only be achieved by electron doping. Specifically, as shown in Fig. 5g and h, electron doping of 0.2 e (0.4 e) and 0.4 e (0.6 e) can induce germanene/GdI $_2$ (SiGe/GdI $_2$) to transition into a p-type half-valley Ohmic contact and p-type overall Schottky contact, respectively. The projected band structure of the graphene/GdI $_2$, germanene/GdI $_2$, SiGe/GdI $_2$ vdWHs with different electrostatic doping are shown in Fig. S9–S11 (ESI†), respectively.

Finally, we discuss the charge injection and valley switching at the K and K' points under the action of M-reversing, strain engineering or electrostatic doping, as shown in Fig. 6. In the intrinsic p-type half-valley Ohmic contact of the graphene/GdI2 vdWH, as shown in Fig. 6a, electrons originating from GdI₂ can be injected into graphene through the K valley (ON), while the K' valley is closed (OFF). In the intrinsic p-type overall Ohmic contact of the germanene/GdI2 and SiGe/GdI2 vdWHs, as shown in Fig. 6e, both the K and K' valleys participate in electron transport (ON), allowing free electron movement between the two valleys. As shown in Fig. 6b and g, by reversing the magnetization direction of Gd from +z to -z, valley polarization is flipped, enabling the switching of the electron transport valley state between the K and K' points. When combined with spintronics, magnetization reversal has the potential to create devices that couple spin and valley states, further expanding the range of possible applications. Adjusting the interlayer distance or electron/hole doping can regulate the contact type of the X/GdI₂ vdWHs to switch the electron transport channels in the K and K' valleys, as shown in Fig. 6c, d and f, h, making them ideal candidates for valley-state logic devices. Fig. 6i and j schematically illustrates a valley-state logic device controlled by two gates (G₁ and G₂), with Dirac semimetals serving as the source and drain, connected by the 2D GdI2 channel. The positive and negative voltages applied to G1 and G2 selectively regulate electron transport between the K and K' valleys, enabling binary logic state encoding of "1" and "0" based on valley polarization. When the electric fields applied by both gates are in the same direction, both regions conduct through the same spin at either the K or K valley, and the device is in the on state ("1"). When the electric fields are opposite, the two regions conduct through opposite spins at the K and K' valleys, and the device is in the off state ("0"). The ability to switch between half-valley and overall Ohmic contacts also facilitates the design of highly sensitive photodetectors that can selectively detect light with different wavelengths or polarizations, thereby enabling efficient photoelectric conversion. In the p-type overall Schottky contact of the X/GdI2 vdWHs, as shown in Fig. 6c and h, due to the presence of the Schottky barriers, the electron transport channels in both the K and K' valleys are closed (OFF). However, the nonlinear current-voltage characteristics of the p-type overall Schottky contact make the X/GdI2 vdWH well-suited for rectifiers and Schottky diodes.

4. Conclusions

In summary, through first-principles calculations, we designed a class of p-type Ohmic contact vdWHs consisting of the valleypolarized semiconductor GdI2 and Dirac semimetals X (X = graphene, germanene, and SiGe). Our binding energy analysis identified the T1-type stacking configuration as the most stable structure among different atomic alignments. Due to strong interlayer interactions and SOC effects, the Dirac semimetals exhibit band splitting and significant bandgap opening at their Dirac points. Meanwhile, the work function differences between GdI₂ and Dirac semimetals drive charge transfer from GdI₂ to the Dirac layers, inducing upward band bending in GdI2 and shifting the Fermi level of the Dirac semimetals. Projected band structure analysis reveals that graphene/GdI2 vdWH exhibits an intrinsic p-type half-valley Ohmic contact, while germanene/GdI2 and SiGe/GdI₂ vdWHs form intrinsic p-type overall Ohmic contacts. Additionally, we demonstrate that interfacial charge transfer and SBHs in X/GdI2 vdWHs can be precisely modulated through vertical strain engineering and electrostatic doping, enabling controlled transitions among half-valley Ohmic, overall Ohmic, and Schottky contact states. Notably, valley-switching ON/OFF behavior at the K and K' points can be effectively regulated, offering a pathway for tunable valleytronic functionalities. This study provides valuable insights into valleytronic interface engineering and the design of valley-polarized semiconductors, paving the way for the development of highly efficient multi-state computing and storage devices with optimized carrier injection and ultra-low power consumption.

Author contributions

Hao Guo: conceptualization (equal); data curation (lead); formal analysis (lead); investigation (lead); validation (lead); visualization (lead); and writing – original draft (lead). Yongqian Zhu: conceptualization (equal); validation (supporting); visualization (supporting); and writing – review and editing (supporting). Jinbo Pan: supervision (lead); resources (supporting); and writing – review and editing (lead). Shixuan Du: resources (lead); supervision (supporting); and writing – review and editing (supporting).

Conflicts of interest

There are no conflicts to declare.

Data availability

The data supporting this article have been included as part of the ESI. \dagger

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